

SIGHT-O-TUNER II

OPERATING MANUAL



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SIGHT- O-TUNER® II INSTRUCTION MANUAL

INTRODUCTION

The Musicalibrator (later renamed the Sight-O-Tuner (SOT)) was originally invented and designed by Dr. Albert E Sanderson in the early seventies as a prototype to tune pianos. The invention led to the application and granting of eight patents on circuit design and the method of measuring inharmonicity to create a tuning that took inharmonicity into account. The patent rights were later licensed to Tuners Supply to produce the Sight-O-Tuner. After a few years went by, there was an attempt by Tuners Supply to change overnight the reimbursement terms of the contract that led to a lawsuit. Those problems with the contract prompted Al Sanderson to redesign and start producing the Sanderson Accu-Tuner® in his basement. By producing the product himself, Dr. Sanderson had control over the quality and quantity of the units produced. Initially Inventronics was repairing the Sight-O-Tuners to help out piano technicians in an attempt to keep quality of the SOT up to Dr. Sanderson's standards.

Jumping forward thirty years, recently the last person repairing the Sight-O-Tuners passed away, and we received quite a few phone calls asking who would repair the Sight-O-Tuners. This got the ball rolling to create a solution. Quite a few of the components in the SOT are no longer available and repairing the original circuit design was not an option. So one of Inventronics employees, Brian Day, started working on the idea of replacing the entire electronics and using some of the circuit designs Inventronics uses in the production of the Accu-Tuners. This is the solution Inventronics has come up with to keep the SOT owners in business until they are ready to step up to the Sanderson Accu-Tuner.

Tuning with the new electronics in the Sight-O-Tuner II (SOT II) is very similar to the previous SOT with two new features:

- 1) The SOT II can automatically set the cents for a Stretch Tuning.
- 2) Coarse cent dial can be set up to jump to the nearest five cent increment, for more accuracy.

GETTING STARTED

When the SOT II is turned on, the SOT II starts in the self-calibrating state for two seconds, two LEDs will be lit, generally at three and nine o'clock, and then automatically switches over ready to tune.

The SOT II will be fully charged when received. The Lithium Ion (Li-ion) battery will function for thirty or more hours before charging is required. This battery is tolerant of deep discharge, and the SOT II will turn itself off at a safe low-battery voltage, shortly after the Lo Battery LED is lit.

LOW BATTERY INDICATOR

The SOT II indicates the low battery similar to the original SOT, the LED between six and nine o'clock will remain lit. Shortly after the LO Batt LED is lit, the SOT II will turn itself off to before a low battery condition can create unstable results.

THE TWO MODES OF OPERATION

The Sight-O-Tuner II has two basic modes of operation:

- 1) The TUNE mode.
 - 2) The Stretch Mode
- 1) When the SOT is first turned on, calibration signal will display for two seconds, and then it enters the TUNE mode.
 - 2) There is a new button between the COARSE and FINE labels on the face of the SOT. Once you have measured the stretch number, press the STRETCH button, the partial and cents deviation for the stretch tuning will automatically be set internally.

THE TUNE MODE

Immediately after exiting from the CALIBRATION mode, whatever the combination of the NOTE, OCTAVE, FINE and COARSE cents knobs are set to is the pitch that the SOT will be tuning. This is essentially what you see is what you get, as long as the STRETCH button is NOT LIT.

STRETCH TUNING

The previous Stretch Calculator slide rule is replaced with the ability of the new microprocessor to set the partial and cents automatically for you. This improvement will make the tuning of a piano quicker and being able to re-check the tuning almost instantaneous. In this mode, the Sight-O-Tuner II creates a 41 note tuning that is derived from the measurement of the stretch number from F4 on the piano being tuned. Every time the note or octave is changed, the computer references the stretch tuning from the memory and sets the partial and cents deviation correctly for that note.

The new SOT has the stretch tuning curves built in for stretch numbers from 2.0 to 9.0, which works out to fifteen different stretch curves are built in for automatic setting of the cents knob.

MEASURING THE F4 STRETCH NUMBER

- 1) Set the Sight-O-Tuner to F5, zero cents in the TUNE mode (stretch button not backlit). Play one string of F4 and use the COARSE cents knob to stop the rotation of the LEDs.
- 2) Turn the OCTAVE knob to step up one octave to F6, and play F4 again, and use the FINE cents knob to stop the rotation of the LEDs. The fine cents knob now displays the F4 stretch number, which is the difference in cents between the second and fourth partials of F4. Please jot down the stretch number for use in step 5 or make a mental note.
- 3) Now set the SOT to note A, octave 4, and both COARSE and FINE cents to zero. Tune the note A4 on the piano or if not tuning to A 440 Hz, offset the cents accordingly.
- 4) Step the SOT up one octave to A 5, play the note A4 on the piano and use the COARSE and FINE cents knob to stop the rotation of the LED's.
- 5) Now press STRETCH button, the STRETCH button will be backlit red, now turn the FINE cents knob to the stretch number you measured in step 2. Now the SOT II will automatically set the CENTS for the selected stretch number. No need to turn either of the CENTS knobs, just set the NOTE and OCTAVE switches to the desired note between C3 and F6. The COARSE knob has no effect on the setting of the stretch number, if the stretch number is 8.0 set the FINE cents knob to -1.0, stretch number of 9.0 set the FINE cents knob to -2.0.
- 6) Now the microprocessor will automatically set the cents for the correct deviation according to the old stretch calculator slide card.

You are all set to start tuning the note C3. To start at any other note between C3 and F6, just proceed to that note with the NOTE and OCTAVE switches.



SOT II with the STRETCH button lit.

STRETCH TUNING PARTIALS

When the SOT II creates a stretch tuning, the program creates the tuning and it is automatically set the SOT II to the correct partial in the following manner. This is illustrated in more detail in the following tables:

OCTAVE	PARTIAL	KEYBOARD	PITCH OF PARTIAL
Octave 3	Fourth Partial	C3	C5
Octave 4	Fourth Partial	F4	F6
Octave 4	Second Partial	F#4	F#5
Octave 5	Second Partial	F5	F6
Octave 5	Second Partial	F#5	F#5
Octave 6	First Partial	F6	F6

Just to reiterate, C3 to F4 fourth partial, F#4 to F5 second partial, F#5 to F6 fundamental partial as shown in the table below.

Piano Note	SOT Automatically listening to		Piano Note	SOT Automatically listening to		Piano Note	SOT Automatically listening to
C3	C5		F#4	F#5		F#5	F#5
C#3	C#5		G4	G5		G5	G5
D3	D5		G#4	G#5		G#5	G#5
D#3	D#5		A4	A5		A5	A5
E3	E5		A#4	A#5		A#5	A#5
F3	F5		B4	B5		B5	B5
F#3	F#5		C5	C6		C6	C6
G3	G5		C#5	C#6		C#6	C#6
G#3	G#5		D5	D6		D6	D6
A3	A5		E5	E6		E6	E6
A#3	A#5		F5	F6		F6	F6
B3	B5						
C4	C6			2 nd Partial			1 st Partial
C#4	C#6						(Fundamental)
D4	D6						
D#4	D#6						
E4	E6						
F4	F6						
	4 th Partial						

STRETCH Tuning from C3 to F6

After the stretch tuning has been selected, (stretch button backlit) tuning can start on any note between C3 and F6. When ready to tune the next note, turn the NOTE and or OCTAVE knobs. For every semitone the SOT will automatically update the partial and cents deviation for the next note, continue this way for the notes C3 to F6. Just to verify: the SOT should be set to the note on the piano you are tuning and the SOT II automatically selects the partial and cents deviation.

Unison Tuning

Unisons may be tuned aurally along with a stretch tuning of the center string, or each string may be tuned individually to the SOT II and the unisons checked aurally later on. The SOT II will do an excellent job of tuning unisons when the strings of a given note are well matched. (They are on

most notes.) The fact that some strings are mismatched makes it extremely important for the tuner to check all unisons aurally when they have been tuned with the SOT II. However, do not try to check the unisons aurally during any pitch raise. Pulling up adjacent strings affects the pitch of the strings that have already tuned. The settling process on a string is not complete until another octave or so has been tuned.

Aural unison tuners should be aware that pulling in two outside strings to the tuned center string will affect the pitch of the center string. The amount is roughly equal to one-fifth of the net pitch change. As a result, when there is more than a few cents pitch change involved, tuning unisons aurally can actually leave them out of tune in the end! To avoid getting into this situation, give the piano a quick pitch raising (or lowering) before trying to do a fine-tuning. If the piano is more than five to ten cents flat, it will actually save time to do a quick pitch raise before attempting to fine-tune the piano.

TUNING BEYOND C3 TO F6

DIRECT TUNING THE HIGH TREBLE

Tuning the high treble with the SOT is relatively easy. The best tuning for each note can be determined by reference to one, two or three already-tuned notes. These notes lay one octave, octave-fifth, and two octaves lower than the note being tuned.

- 1) Set the SOT II to the NOTE and OCTAVE of the note being tuned (in TUNE mode).
- 2) Play the reference notes one at a time and see how they look on the rotating LEDs.
- 3) Turn the CENTS knob up or down until a cents setting that is a good compromise between the reference notes. A cents setting where some of the reference notes rotate slowly sharp and some rotate slowly flat.
- 4) Then tune the note.

Tuning is more challenging in the last octave because a good compromise may be impossible to find. Decide which interval will take priority and tune mainly to satisfy its requirements. At this point many tuners stick to the single octave, but tune one or two cents wide. Others prefer to tune the double octave, which gives a sharper top end, or the octave-fifth, which is quite a bit sharper. The choice is up to personal taste and the customer preference.

DIRECT TUNING THE BASS

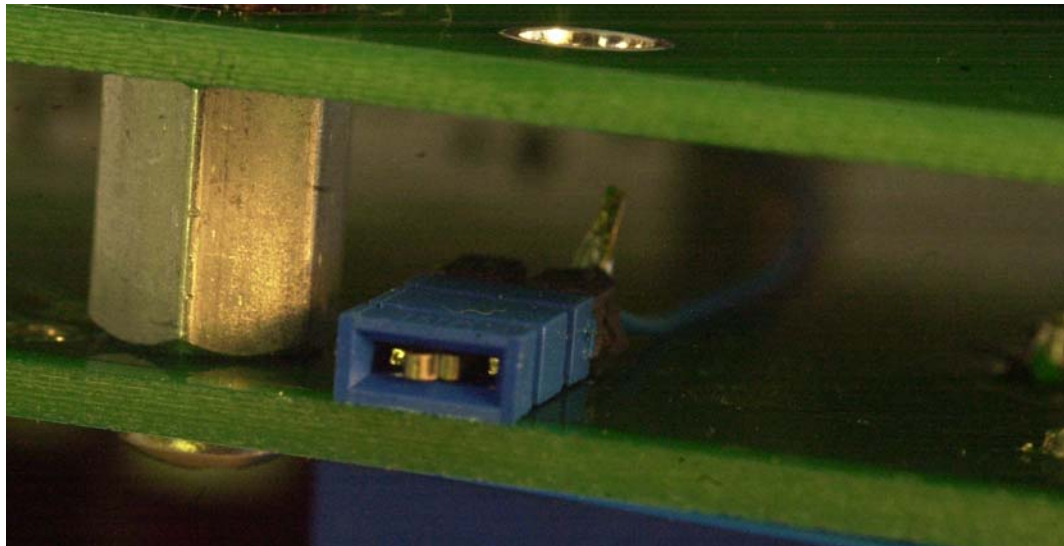
Tuning the bass is similar in principle to tuning the high treble. Set the SOT II with reference to several previously tuned notes and compromise among them to place the note being tuned.

The best reference notes lay an octave, an octave-fifth, and a double octave-fifth higher than the note being tuned. To use these reference notes, set the SOT II a double-octave-fifth higher than the note being tuned (on its sixth partial).

- 1) Play each reference note one at a time.
- 2) Turn the CENTS knob until a good compromise setting is found, one where some reference notes are rotating slightly flat, others slightly sharp.
- 3) Tune the note.
- 4) Continue this procedure all the way down to A0.

In contrast to the situation in the high treble where the three tests diverge, the three bass tests usually work nicely all the way down to A0.

Changing the COARSE cents control, if you would like to increase the accuracy of the SOT II, you can move a jumper to have the coarse cents control jump to the nearest five cent increment.



With the jumper in the position above, shorting out the two pins, the coarse cents knob will jump to the closest five cent increment. The jumper is physically located beneath the FINE cents trimmer on the PC board.

Cents Offset for Hz at A4

Frequency of A4	Cents Offset
446	23.5
445	19.6
444	15.7
443	11.8
442	7.9
441	3.9
440	0.0
439	-3.9

Frequency of A4	Cents Offset
438	-7.9
437	-11.8
436	-15.8
435	-19.8
430	-39.8
420	-80.5
415.3	-100.0
415	-101.3

Formula for calculating cents offset of A4 at 420Hz: $\text{Log}(420/440, 2) * 1200 = -80.54$

INPUT-OUTPUT JACKS

There is one input for charging the battery and one output jack on the SOT II. The output jack can be set up for a variety of outputs. The standard use for the jack when originally manufactured was for an audio input.

AUDIO IN: An electrical audio input jack. Signals are fed into this phono jack for silent measurements of pitch, or tuning electronic musical instruments. This input is suitable for levels from 0.01 to 10 volts.

The SOT can also be set up with the output jack to do either of the following options:

OSC OUT: A phono jack, which puts out a modified saw tooth wave (one that is quite pleasant to listen to) at the pitch called for by the settings of the SOT II controls. This has a variety of uses. The frequency calibration of the instrument can be checked with this output. It can also be fed into

an amplifier and broadcast, to give an aural pitch standard for any purpose. One purpose is an aid to fast piano chipping or rough pitch raising.

FLTR OUT: A phono jack output from the audio filter. The audio filter amplifies sounds whose pitch corresponds to the pitch selected on the SOT II. It is useful for listening to the beats at the coincident partial of two notes forming a musical interval. This feature can be a valuable training aid for aural tuners.

BAT CHGR: Located on the ON-OFF end of the SOT, this jack is used for charging the battery. DO NOT use battery chargers other than ones recommended for the SOT II, even when the plug is compatible with the SOT II jack, because voltage ratings and polarity can differ, too high voltage may damage the battery charger circuit in the SOT. (The Radio Shack model 273-355 is a compatible unit.) Battery charger specifications, output 9 volts DC, 800 plus milliamps, 2.1 mm barrel, positive on the inside of the barrel, negative on the outside. The battery will be eighty percent charged after a period of five and a half hours, completely saturated after eight hours.

BATTERY CARE

LITHIUM ION

The battery used in the SOT II, is a Lithium Ion (Li-ion) battery. The new Li-ion will run the SOT for 30 plus hours, and can be recharged hundreds of times. To achieve the longest battery life we do recommend that the SOT II be used until the low battery is displayed. Li-Ion batteries do not benefit from nightly charging, but will last longer if used to capacity before recharging.

BATTERY CHARGING CIRCUIT

The Li-Ion battery in the SOT II has a large capacity and presently is supplied with a 9.0 Volt, 800 milliamp AC adapter. When the SOT II charger is first plugged in, the red LED will be lit while the battery is charging in the high current mode. The battery will charge at high current for roughly five and a half hours before stepping down to a trickle charge stage. When the SOT shifts down to the trickle charge stage the red LED will no longer be lit. The battery is charged to roughly eighty percent during the high current charging and gets topped off with the trickle charging. Inventronics still recommends charging the SOT II overnight, but the majority of the charging occurs in the first five and a half hours.

ONE YEAR WARRANTY

INVENTRONICS offers a 1-year warranty from date of purchase, on parts and labor. We will repair or replace the SOT II, as determined at the factory, should it be found defective. This warranty is not transferable, and applies only to the original purchaser of the equipment. Damage from the result of misuse, modification, or tampering with the equipment will void this warranty.

APPENDIX A

Concise Step-by-Step Tables of Standard Routines

1. Measurement and Storage of F4 Stretch Number:

TURN ON SOT, NOTE=F, OCT=5, CENTS=0.0, tune F4 to stop LEDs,

OCT up to F6, CENTS up to stop LEDs, PRESS STRETCH button.

Ready to start tuning from C3 to F6.

APPENDIX B

Cents Tables for Non-equal Temperaments

Pythagorean Temperament.

A	0.0	Db	-15.6	F#	5.9
A#	13.7	D	-2.0	Gb	-17.6
Bb	-9.8	D#	11.7	G	-3.9
B	3.9	Eb	-11.7	G#	9.8
C	-5.9	E	2.0	Ab	-13.7
C#	7.8	F	-7.8		

The usual practice is to use only the above flats.

Meantone Temperament

A	0.0	Db	27.4	F#	-10.3
A#	-24.0	D	3.5	Gb	30.8
Bb	17.1	D#	-20.5	G	6.8
B	-6.8	Eb	20.5	G#	-17.1
C	10.3	E	-3.4	Ab	23.9
C#	-13.7	F	13.7		

The usual sharps and flats are C#, F#, G#, Bb, and Eb.

Marpurg's Temperament 1.

A	0.0	C#	0.0	F	0.0
A#	5.9	D	5.9	F#	5.9
B	3.9	D#	3.9	G	3.9
C	2.0	E	2.0	G#	2.0

Werckmeister III, Correct Temperament No. 1

A	0.0	C#	2.0	F	9.8
A#	7.8	D	3.9	F#	0.0
B	3.9	D#	5.9	G	7.8
C	11.7	E	2.0	G#	3.9

Kirnberger III, Corrected Temperament

A	0.0	C#	2.0	F	9.8
A#	7.8	D	3.9	F#	2.0

B	0.0	D#	5.9	G	7.8
C	11.7	E	-2.0	G#	3.9

Young's Temperament No.1

A	0.0	C#	-3.9	F	3.9
A#	2.0	D	2.0	F#	-5.9
B	-3.9	D#	0.0	G	3.9
C	5.9	E	-2.0	G#	-2.0

Vallotti or Fairchild Temperament

(REF: Piano Technicians Journal, Oct. 82, p.20.)

Steve Fairchild independently developed this temperament in 1982 while looking for a temperament to smooth out the simple keys on small pianos. It greatly reduces the harshness caused by excessive inharmonicity, and for that reason could also be called the "Piano Teacher's Delight" temperament.

A	0.0	C#	0.0	F	7.8
A#	5.9	D	2.0	F#	-2.0
B	-3.9	D#	3.9	G	3.9
C	5.9	E	-2.0	G#	2.0

Cents Offset for Hz at A4

Frequency of A4	Cents Offset
446	23.5
445	19.6
444	15.7
443	11.8
442	7.9
441	3.9
440	0.0
439	-3.9

Frequency of A4	Cents Offset
438	-7.9
437	-11.8
436	-15.8
435	-19.8
430	-39.8
420	-80.5
415.3	-100.0
415	-101.3

Formula for calculating cents offset of A4 at 420Hz: $\text{Log}(420/440, 2) * 1200 = -80.54$

APPENDIX C

Aural and Visual Tuning

(The best of both worlds)

By James W. Coleman, Sr.

Owen Jorgenson wrote the definitive work on temperaments and tuning. In his book "Tuning the Historical Temperaments" he traces the natural progress of aural tuning systems from the Pythagorean and Just Intonation systems through several Meantone temperaments to the Well temperaments and the Equal temperament. It is this last system in which most piano technicians are engaged. The basis of this system is the need or desire to be able to play in all keys with equally out of tune parallel intervals. This need was borne out of the practice of composers who became far ranging in their tonalities of a particular composition.

The earliest popular approaches to tuning the equal temperament involved tuning a series of twelve 4ths or 5ths such that each 5th was narrowed slightly and each 4th was widened slightly in such a

way that they were all equally out of tune. The difficulty with this approach was that it took 12 steps before one could tell if he was doing alright.

More recent approaches to equal temperament involve one or two test intervals for each step taken in the tempering system. More care is being given to insure that each interval (such as the minor 3rds, major 3rds, 4ths, 5ths, minor 6ths, major 6ths) is equally tempered and is compatible with all its parallel similar intervals. Some of the more popular recent temperament systems are by George Defebaugh, Bill Stegeman, Dr. Al Sanderson (2 octave A-A temp) James Coleman (F-A temp) and Mark Peele (10th temp). These may be seen demonstrated at various Piano Technician's Guild Institutes, Conferences and Seminars.

Since the Stretch Calculator tunings involve the accurate tuning of the 4th partial of each note in the F-F temperament, all the intervals which involve the 4th partials will be beautifully tempered (such as major 3rds, 4ths). Other intervals such as minor 3rds, major and minor 6ths, which are involved with higher order partials, will also be beautifully tempered. Since the greatest irregularity in partial alignments occurs in the 1st, 2nd, and 3rd partials, there may be some slight unevenness heard in the octave and 5ths.

Now, by the simple practice of playing certain test intervals while tuning with the Stretch Calculator mode, one can have a double check on his aural test as well as assuring that the visual judgments are more accurate. If one tunes the stretch tuning system from top to bottom or at least from C5 down, when the 4th 1/2 step down is achieved, a major 3rd aural test is available without the upper note interfering with the LED display. In arriving at the seventh 1/2 step down, a 5th is available for aural judgment without LED interference from the upper note of the interval. This 5th interval can be followed on down to C3. One may notice a slight variation in the sound of the 5ths especially as one approaches the lower area of the scale. Sometimes this is merely due to the slipping or instability of the previously tuned upper note of the 5th. But, with the shorter scaled pianos, irregularity of the lower partials may cause the beat frequency to be greater than expected. At this point one may make a decision to alter the lower note to smooth out of the 5th interval (which of course may change the beat rate in other intervals based on this lower note). By doing this judiciously one can have a better tempering than can be had with either aural or visual methods alone.

APPENDIX D

What are Partial and Beats?

By James W. Coleman, Sr.

A piano string has a series of partials (sometimes erroneously called harmonics) which are approximately whole number multiples of the fundamental frequency (first partial). For example the 3rd A on a piano (counting from A0, A1, A2) has a theoretical frequency of 110 cycles per second (or Hertz). If it is multiplied by 2, you have 220 Hz (2nd partial). If one places his finger lightly on the middle of a string, he can force it to vibrate at its 2nd partial. If A2 is lightly touched at a distance of 1/3 the length from one end after the note is played, the string will be forced to vibrate at its 3rd partial (approximately 330 Hz which is 3 times the fundamental pitch). One can continue to divide the string by 1/4, 1/5, 1/6, 1/7, 1/8, etc. This will cause the string to sound at its 4th, 5th, 6th, 7th, and 8th partials respectively.

In order to further clarify, let me say that when a string is forced as above to vibrate in three parts by touching it at the 1/3 point; we say that this is the 3rd partial because one can see the string breakup into 3 parts with 2 nodal points in between. At the same time one notices that the pitch jumps one octave plus a 5th (19 half-steps above).

One should learn the note location for the partial series for each note of the chromatic scale. Here are the notes that correspond to the locations of the first 12 partials of the note Middle C.

C4 C5 G5 C6 E6 G6 Bb6 C7 D7 E7 F#7 G7

Oct 5th 4th 3rd 3rd 3rd 2nd 2nd 2nd 2nd half

When one is listening to various tempered intervals, there is at least one particular area where one can hear the beat phenomenon between coincident partials of the two notes. For example: when listening to the 5th (F3-C4), these 2 tones have partials which occur in close proximity to the note C5 (the 3rd partial of F and the 2nd partial of C). These are called the first of lowest coincident partials. If there is a slight difference in the pitch of the two coincident partials, one can hear a slight waver in the tone. This is called the beat phenomenon at the pitch of C5. It is the difference of frequency or Hz of these two partials. One can calculate the beat speed if one knows the cents reading of each of these two partials. The following formula is helpful to convert cents difference to beats per second!

Beats = ref. note Hz x 2 raised to (upper cents deviation/1200) minus ref. Hz x 2 raised to (lower cents dev./1200).

The reference note frequency can be found in charts, but it is so easy to calculate using the 1/12 root of 2, which is the half step ratio. If we need to know the Hz of C5 we merely multiply A440 times 1.0594631 three times to get 523.2251. In the process we find A# at 466.164, B 493.883. If we wish to find Hz below A440 we divide by 1.0594631. G# equals 415.305, G = 391.995 etc.

Now let's use the formula above to find the beat rate of the interval F3-A3 (Major 3rd). The 5th partial of F3 is at the note location of A5. The 4th partial of A3 is also near A5. When properly tuned, on most pianos they will create a beat rate of approximately 7 beats per second. Let's say that the 4th partial of A3 reads +3.7 cents and the 5th partial of F3 reads -10 cents at the reference note of A5 (880 Hz). At A5, -10 cents is the same as G# +90 cents since we have 100 cents per half step. Now, taking the higher reading first, we have

Ref Hz 880 x (2 raised to (3.7/1200)) = 881.883

Ref Hz 830.61 x (2 to (90/1200) power) = 874.932

This leaves us with a difference of 6.95 Hz, which is the beat frequency of the lowest coincident partials of these two notes.

With the aid of a scientific calculator one can easily compute the beat rate of any interval. Dr. Sanderson has an excellent set of notes on how to tune a beautiful 2 Octave Temperament by carefully measured intervals using either aural principles or machine techniques. You may find it interesting to measure your resulting interval widths after setting a careful machine tuning or vice versa, you may find it more interesting to measure interval widths after very carefully tuning by ear. (See Appendix E)

APPENDIX E

The Two-Octave "A" Temperament

By Dr. A.E. Sanderson

The two-octave A temperament is probably the first temperament designed to take into account the inharmonicity of pianos strings. Inharmonicity not only changes the beat rates from their theoretical values for all intervals on a piano, it also creates impossible tuning conflicts as well. The simple octave splits up into different kinds of octaves, depending upon which pair of coincident partials are tuned to zero beat. Even the single, double, and triple octaves are incompatible intervals on a piano, and can only be tuned to sound "as good as possible," not perfect, because inharmonicity makes perfection literally unattainable.

The two-octave A temperament is tuned from the "outside in." That is, the wide intervals, two octaves and the double octave, are tuned first. This is done so that octave tuning problems with a piano will show up at the earliest possible stage when they are relatively easy to correct with small compromises. Many pianos have, unfortunately, incompatible tuning requirements, and by tuning

the three A's first, we can establish a double octave and two octaves that fit as well as is possible both with each other and with the scale of the given piano.

Next we subdivide this wide interval into six equal parts by tuning six contiguous major thirds that fit between the three A's perfectly. Finally, with every fourth note already tuned, we fit the three missing notes within each major third primarily by tuning a pattern of thirds and fourths.

Tuning wide intervals first and then subdividing them has important advantages over the usual methods of building up wide intervals by tuning a succession of narrow ones. In the first place, it guarantees that the wide intervals will be as harmonious as possible, and that the narrow intervals will be adjusted or forced to be compatible with them. Secondly, small errors in tuning narrow intervals cannot add up to become large errors in the wide intervals, no matter how difficult the scale of the piano. This not only leads to greater accuracy on well-scaled pianos, but also greatly reduces the number of problems associated with tuning poorly scaled pianos.

Direct-Interval Tuning

Direct-interval tuning is a way of using the Sight-O-Tuner II that exactly simulates the way fine aural tuners tune by ear. Each interval is tuned by setting its width to a specified number of cents, which is verified by a direct measurement. Hence the term "direct-interval tuning". The sequence of intervals followed is circular, just as in aural tuning, and this makes it quite easy for the tuner to check each interval aurally as it is tuned. (If you are not familiar with measuring the width of intervals in cents, refer to the section entitled "Measuring the Width of Musical Intervals").

First, two single octaves and the double octave are tuned using direct-interval measurements. Second, the double octave is subdivided in six equal parts with a set of contiguous major thirds that mathematically fit this span perfectly, as determined by direct interval measurements. This leaves every fourth note tuned, and the three untuned notes within each major third are then tuned with fourths and thirds, again by direct interval measurements. Follow the step-by-step procedure below, and be sure to check all intervals aurally as you tune:

Step 1. Tune A4 to zero cents, and A3 from A4 as a 2-4 octave 1 cent wide. (Refer to Appendix H if you are not familiar with the different kinds of octaves.)

Step 2. Tune A2 from A3 as a 3-6 octave 1 cent wide. Check the A2-A4 double octave, and if it is more than 4 cents wide, divide the excess by three and narrow both octaves by this amount. (E.g., if double octave is 5.5 cents wide, $5.5 - 4 = 1.5$, divide by 3, and narrow both octaves .5 cent.)

Step 3. Tune three major thirds of equal cents width between A2 and A3. You must first guess how wide to tune them and then see how the guess works out and revise it if necessary. A good first guess is 13.5 cents. So tune F3 from A3 13.5 cents wide, then C#3 from F3 13.5 cents wide. Measure the width of the A2-C#3 third. If it is also 13.5 cents wide, you were lucky and these three thirds are the correct width on the first guess. If you were not so lucky, average the three thirds (two of which were 13.5 cents wide), and tune all three to this average value by retouching C#3 and F3.

Step 4. Now tune C#4 from A3, and F4 from C#4, as thirds of this same value. You have now tuned five contiguous thirds all the same width, a width that fits exactly the A2-A3 octave. To see whether this width fits the A3=A4 octave, measure the width of the last third, F4-A4. If this agrees with the other thirds, you were lucky again and these six thirds are all tuned. If you weren't lucky, take the discrepancy of the last F4-A4 third, divide it by 3, and move F4 by this amount in the direction that will reduce the discrepancy. (E.g., if you had five thirds at 13.5 cents, and the last was 12 cents the discrepancy is 1.5 cents. Take one-third of this, 0.5 cents, and move F4 flat by this amount. This leaves you with four thirds at 13.5, one at 13, and one at 12.5. This is quite reasonable on that "inharmonic instrument," the piano).

Step 5. Now every fourth note is tuned from A2 to A4. Fill in the missing notes between F3 and C#4 to get a nine-note mini-temperament. You must now take a guess at the width of the fourths, try it on the mini-temperament, and revise it as necessary to make the fourths fit with the thirds, whose width you already know. A good first guess for fourths is 2.5 cents. Tune up a fourth from F3 to A#3 down a third from A#3 to F#3, up a fourth from F#3 to B3 and stop. Now tune down a fourth from C#4 to G#3, up a third from G#3 to C4, down a fourth from C4 to G3 and stop. You have filled in the six missing notes of the mini-temperament, now you can tell whether your guess on the width of the fourths was correct from the width of the G3-B3 third, which is the check interval.

Step 6. Measure the width of the G3-B3 third and compare it to what it should be. If it is smaller than the other thirds, your fourth guess was also too small, and vice versa. The size of the error in the fourths equal one-quarter the error in the G3-B3 check interval because four fourths were tuned to get to the check interval.

Step 7. Retune the mini-temperament as in Step 5 with the new correct value for the widths of the fourths. Check it aurally to see that you have five perfectly rising thirds, and four equally good fourths. This result can always be achieved even on the most poorly scaled piano, since we have not been asked to make any compromises up to this point.

Step 8. Tune outwards from the mini-temperament with major thirds down to A2 and up to A3. The thirds tuned downwards are constant width but the thirds tuned upwards may have to be calculated if their width varies. Use straight-line interpolation based on the three known thirds in the A3-A4 octave, to get numbers for the missing thirds. (E.g., in Step 4 these three thirds, A3-C#4, C#4-F4 and F4-A4 were 13.5, 13, and 12.5 cents, respectively. Straight-line interpolation gives values of 13.4, 13.3, and 13.1 for A#3-D4, B3-D#4 and C4-E4, and 12.9, 12.8, and 12.6 for D4-F#4, D#4-G4 and E4-G#4, respectively).

Step 9. The electronic tuning of the two octaves A2-A4 is now complete. A very careful aural check is advisable at this point. Pay particular attention to the fourths, which are wider than theoretical owing to the effects of inharmonicity. The fifths are purer than theoretical for the same reason, and rarely cause any trouble.

Aural Tuning

The two-octave "A" temperament may be tuned aurally with exactly the same note-tuning sequence. This makes it easy to check an electronic tuning aurally at every step--very helpful in avoiding errors. Aural tuners can study and possibly improve their tuning by using the SOT II to measure the width of tuned intervals after setting this two-octave temperament very carefully by ear.

Step 1. Tune A4 to 440 Hz. Use F2 as test note, 17th to fork should beat same as 17th to A4. Tune A3 from A4 as a 2-4 octave, 1½ beat wide. That is, the tenth should beat 1½ beat per second (bps) faster than the third.

Step 2. Tune A2 from A3 as a 3-6 octave 1½ beat wide. That is, the major sixth should beat 1½ bps faster than the minor third.

Step 3. Check the double octave, a 1-4 interval to be less than 1 beat wide. That is, the 17th beat should be less than 1 bps faster than the third. If the double octave is too wide, compromise both octaves slightly to get an acceptable double octave.

Step 4. Divide the A2-A3 octave into three equal parts by tuning C#3 and F3. These thirds can be tested very accurately with the contiguous thirds test. This test states that two contiguous thirds must have relative beat rates in the ratio of 4 to 5, that is 4 beats of the lower one require the same amount of time to complete as 5 beats of the upper one. This test then does not require knowledge of beats per second, only a good sense of rhythm or tempo. In this case, C#3 and F3 are correctly

tuned when 4 beats of A2-C#3 occur at the same tempo as 5 beats of C#3-F3, and in addition, 4 beats of C#3-F3 occur at the same tempo as 5 beats of F3-A3.

Step 5. Now tune C#4 and F4 to divide the A3-A4 octave into three equal parts with thirds. You may have to taper the width of the thirds downwards slightly in the upper octave on account of the inharmonicity of the piano.

Step 6. Check that the three major tenths formed on the seven notes tuned so far also in the ratio of 4 to 5. Also check the C# and F octaves with both the third-tenth and minor-third-sixth tests. Scale problems will show up at this stage, and it may be necessary to compromise slightly the perfectly rising thirds to get satisfactory octaves and tenths.

Step 7. Fill in the six untuned notes between F3 and C#4 to get a nine-note mini-temperament, but be sure not to change already tuned notes. Tune up a fourth from F3 to A#3, down a third from A#3 to F#3, up a fourth from F#3 to B3 and stop. Then tune down a fourth from C#4 to G#3, up a third from G#3 to C4, down a fourth from C4 to G3 and stop. Check the G3-B3 third, which is the test interval for this tuning. If it is too small, you must expand your fourths, and vice versa. With just nine notes to worry about, it is always possible to get five perfectly rising thirds and four matched fourths no matter how poorly scaled the piano may be. The beat rates may not be very close to theoretical, but they will be right for the given piano and its inharmonicity characteristics. So tune the piano, and let the beat rates fall where they may!

Step 8. Tune down to A2 and up to A4, and use the contiguous third test to place each note initially. Check each note with the fourth and fifth, and then the major sixth and octave as they become available. The final result should be two octaves tuned with rising thirds all the way, with all fourths quite even and acceptable, and with all fifths nearly pure.

APPENDIX F

Contiguous-Interval Tuning Tests for Electronic Piano Tuners

By Dr. A.E. Sanderson

Two contiguous musical intervals are intervals that touch each other, in other words, share the note in the middle. Tests that use contiguous intervals are easy to learn and use, and tell the tuner explicitly which notes are at fault and what to do to correct them.

Contiguous major thirds will beat in the ratio of four to five because the major third itself consists of two notes whose frequencies are in the ratio of four to five. Displacing any interval up the keyboard will speed it up theoretically in the ratio of the frequencies of the two root notes involved. Therefore two contiguous major thirds should beat in the ratio of four to five, two contiguous minor thirds in the ratio of five to six. Similarly, two contiguous fourths should beat in the ratio of three to four and two contiguous fifths in the ratio of two to three. However, on the piano this theoretical relationship holds well only for the major and minor thirds. The fourths and fifths are so strongly affected by inharmonicity that these contiguous intervals beat at almost the same speeds.

Using the above facts, we can develop a test for one note of the piano at a time. Take C4 for example. Play down a third and up a third G#3-C4 and C4-E4, keeping time at the rate of four beats of the lower one, and then at five beats of the upper one. Think of it as four beats to the measure, followed by five beats to the measure. The tempo of the two kinds of measures should agree. If the upper beat rate is too fast, it indicates that C4 may be flat, and vice versa.

Before moving C4, we need more evidence. Play down a fourth and up a fourth, G3-C4 and C4-F4, and listen for near equality of the beat rates, or an upper beat rate just slightly faster than the lower. If C4 is flat the upper fourth will be faster than the lower, and vice versa. If both the fourth

test and the third test indicate the C4 is flat, this is very strong evidence that C4 should be moved. But to nail down your decision, you can add a contiguous fifth test as well.

To check contiguous fifths, play down a fifth and up a fifth, F3-C4 and C4-G4. If C4 is flat, the lower fifth will beat faster than the upper.

In our example, we have now used three tests, and six other notes to check up on one note. If all the tests indicate that C4 is flat, then it is a good idea to move C4. If some tests say flat and some say sharp, then leave C4 where it is and go on to test other notes. Eventually you will find the main culprit or culprits, the notes for which all three tests say the same thing. Move these notes without hesitation. Your temperament will improve steadily as you find and correct each note that fails all three contiguous tests.

The range of this contiguous-interval test is at least from C3 to C5, a two-octave span. After tuning the whole piano, unisons and all, start applying this test at C3. Move up one semitone at a time, and correct any note that fails all three tests before moving on. Go up to C5 this way. If you like, you may make a second pass from C3 to C5 and polish your tuning even more. Eventually you will reach the point where no notes can be improved upon, and at that point you will have an extremely fine tuning. A supertuning if you will!

APPENDIX G

Octave Tuning

By Rick Baldassin

Tuning octaves with the Accu-Tuner can be directly related to tuning octaves aurally with specific interval tests. These interval tests and electronic setting instructions have been included here for three primary reasons: 1) So that aural tuners will know which Accu-Tuner settings correspond to the interval tests they have been using. 2) So that Accu-Tuner users may expand their aural tuning abilities by checking aurally with interval tests, and 3) To raise in general the level of knowledge relating to octave tests, electronic setting instructions, and their use in piano tuning.

Knowing that there are several types of octaves, aural tests and electronic setting instructions are necessary to insure that the appropriate type is being tuned in a given area of the piano. Since only one type is in tune at a time, and so rare is the exception, the tests and setting instructions for one type only should be used at a time. The exception, of course, would be in a transitional area, changing from one type to another.

Two different aural tests along with the electronic setting instructions have been provided so that the findings may be double-checked. Since the aural tests employ the use of intervals for comparison, both expanded and contracted, and either the upper note or lower may be the reference to which we are tuning, four classifications of aural tests result. Be sure to note the Classification for each test so as to correctly interpret the findings and make the proper adjustments in tuning the octave.

CLASS A: Lower note is the reference note. If the beat rate between the test note and the upper note is *too slow* as compared to the beat rate of the test note and the reference note, *raise the upper note*. If the beat rate with the upper note is *too fast*, *lower the upper note*.

CLASS B: Upper note is the reference note. If the beat rate between the test note and the lower note is *too slow* as compared to the beat rate of the test note and the reference note, *raise the lower note*. If the beat rate with the lower note is *too fast*, *lower the lower note*.

CLASS C: Lower note is the reference note. If the beat rate between the test note and the upper note is *too slow* as compared to the beat rate of the test note and the reference note, *lower the upper note*. If the beat rate with the upper note is *too fast*, *raise the upper note*.

CLASS D: Upper note is the reference note. If the beat rate between the test note and the lower note is *too slow* as compared to the beat rate of the test note and the reference note, *lower the lower note*. If the beat rate with the lower note is *too fast*, *raise the lower note*.

The object in each case is to obtain an equal beat rate between the upper and lower notes of the octave, and the test note. Each test is given a name corresponding to the intervals employed in the test. In naming the intervals, "P" denotes a so-called "Perfect" interval, "M" denotes a "Major" interval, "m" denotes a minor interval, "A" denotes an "Augmented" interval, and "d" denotes a "diminished" interval. It must be noted that some of these intervals are very hard to hear in the bass region of the piano. These checks, however, are still valid. To make use of these checks, hold down one of the octave notes and the test note without playing them. (You may have to use the sostenuto pedal in some cases). Play the strike note with a staccato blow. Repeat this procedure with the other octave note and the test note. When the two beat rates are the same, the type of octave, which has been tested for, will have been tuned. The strike note in all cases is the note listed in the electronic setting instructions for that particular type of octave.

Octave Type	Aural Tests	Classifications	Electronic Setting Instructions	Area Generally Used
2:1	M10 - M17 P5 - P12	A C	on the upper note	Treble
4:2	M3 - M10 P4 - P5	A,B C,D	octave above the upper note	Midrange
6:3	m3 - M6 P12 - P5	B B	twelfth above the upper note	Midrange, Bass
8:4	m6 - M3 P11 - P4	B D	two octaves above the upper note	Low Bass Medium Pianos
10:5	M6 - m3 A4 - d5	D B	seventeenth above the upper note	Lower bass Large pianos
12:6	m10 - m3 P19 - P12	B B	nineteenth above the upper note	Lower bass Large pianos
4:1	M3 - M17 P4 - P12	A C	on the upper note	Midrange, Treble
8:2	m6 - M10 P11 - P5	B D	octave above the upper note	Bass

SIGHT-O-TUNER II SPECIFICATIONS

NOTE RANGE:

9 Octaves. C1 through B 9 (A4 = 440.00 Hz).

CENTS RANGE:

±62.5 cents with ±0.1 cents accuracy throughout the scale.

CALIBRATION ACCURACY:

Built-in 440.00 Hz crystal frequency standard for self-calibration, accurate to ±0.1 cents.

DISPLAYS:

Rotating light-emitting-diode (LED) display for continuous analog FLAT or SHARP tuning indicator. Separate LED wide-range sharp/flat indicator.

